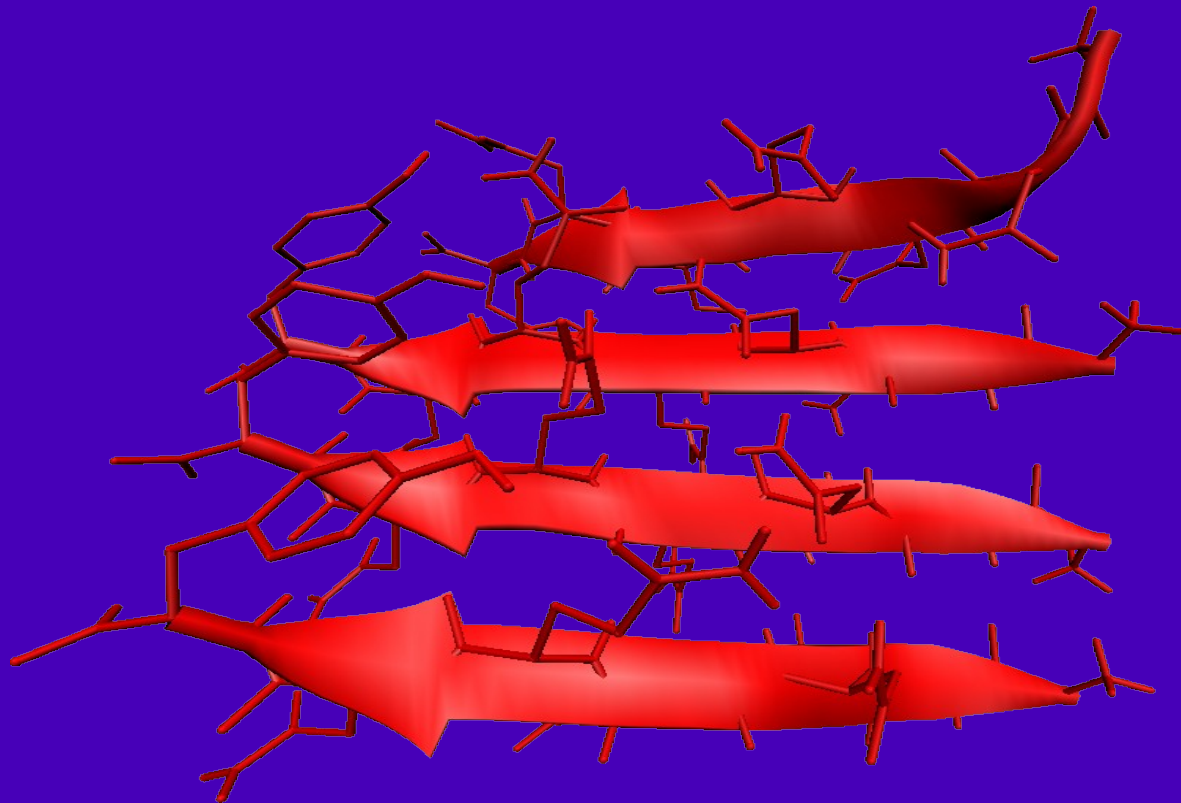


Exploring the Energy Landscape for Amyloid Formation



Telluride, 4th April 2007

Birgit Strodel
University of Cambridge
Department of Chemistry

What are Amyloid Fibrils ?

- **Amyloid** fibrils are encountered in several **diseases** such as **Alzheimer's**, **prion** diseases, or **Parkinson's**.



Sheep infected with **Scrapie**.



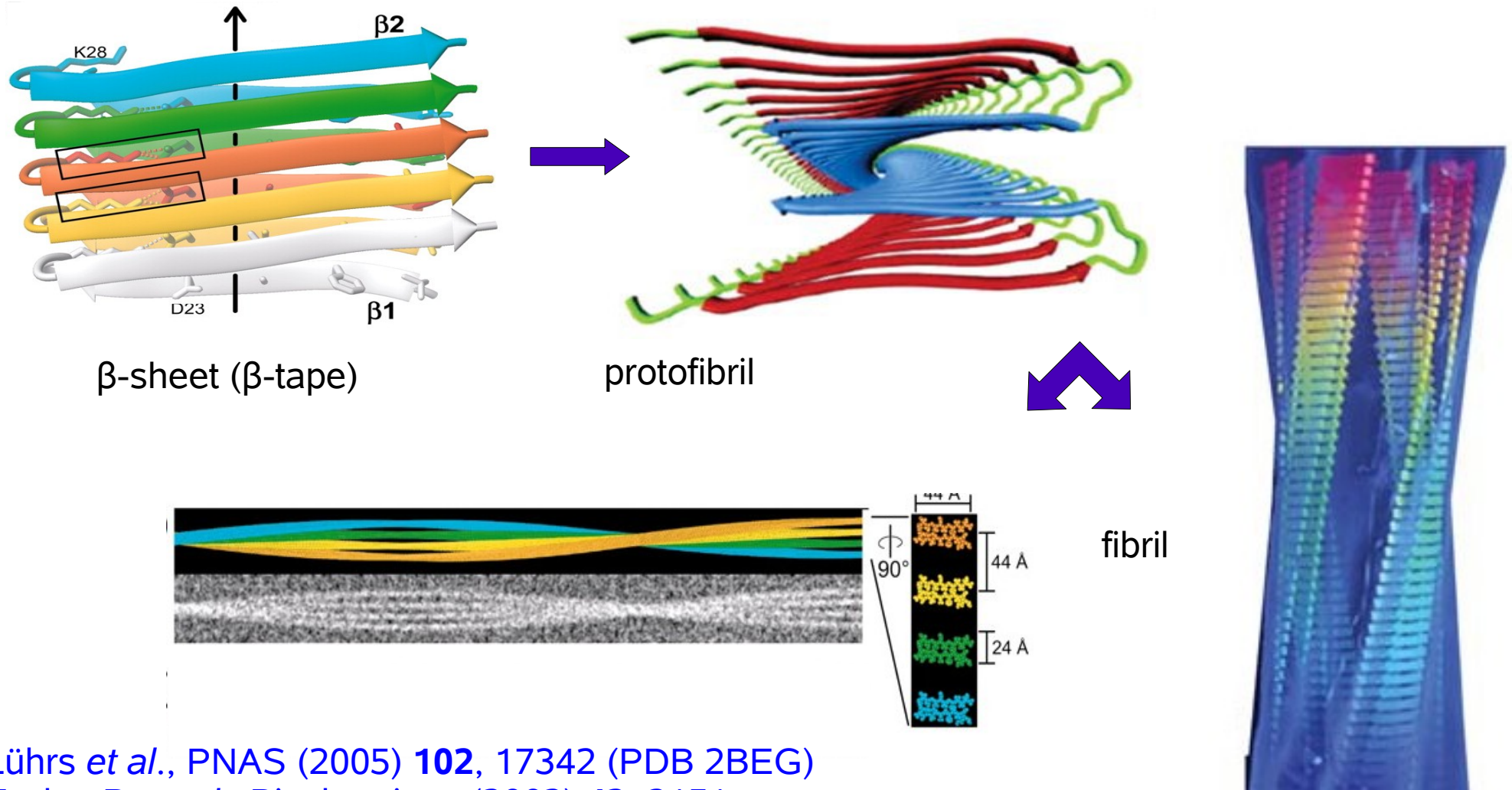
Fore people in Papua New Guinea infected with **Kuru** (“laughing death”) which is caused by their ritual cannibalism.

- Not only the 20 or so proteins associated with clinical disorders form amyloid structures; it now seems to be a **generic feature of polypeptide** chains.
- An increasing number of proteins have been found to form **amyloid fibrils** that have **functional** rather than disease-associated properties.
- For neurodegenerative diseases there is evidence that **soluble oligomers** - the **precursor** stage in fibril formation - are the **cytotoxic** agents.
- For a recent overview, see [F. Chiti & C.M. Dobson, Annu. Rev. Biochem. 75, 333-366 \(2006\)](#)

Structure of Amyloid Fibrils

Amyloid aggregates all share a common **cross β -sheet structure** with the β -strands perpendicular to the fibre axis and the β -sheets propagating along the direction of the fibre.

Example : A β (1-42)



Lührs *et al.*, PNAS (2005) **102**, 17342 (PDB 2BEG)
Tycko, R. *et al.*, Biochemistry (2002) **42**, 3151

Methods

Methods

Motivation : We want to study the **early steps** of the **amyloid self-assembly**. The questions which we would like to address are

- i) What are the **driving forces** for amyloid formation?
- ii) What are the **pathways** for amyloid formation? Are there **different** self-assembly **mechanisms** for different amyloidogenic peptides?
- iii) Is a **reversal** of the early oligomerization process possible?

Our **approach** is as follows:

- All-atom description for the peptide: **CHARMM19** and the **EEF1** implicit solvent potential
- **Basin hopping (BH)** for global optimization of the oligomers.
- **Replica exchange molecular dynamics (REMD)** to calculate the **free energy surface** as a function of suitable order parameters.
- To identify the reaction coordinate we perform **Discrete Path Sampling (DPS)** between different minima of the free energy surface.
- From the DPS phenomenological **two-state rate constants** between ensembles of local minima can be obtained, which are **compared to experiment**.

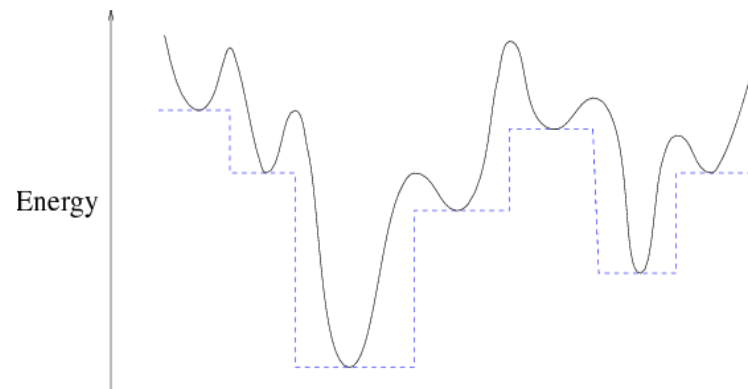
Methods

Basin hopping : Monte Carlo with minimization

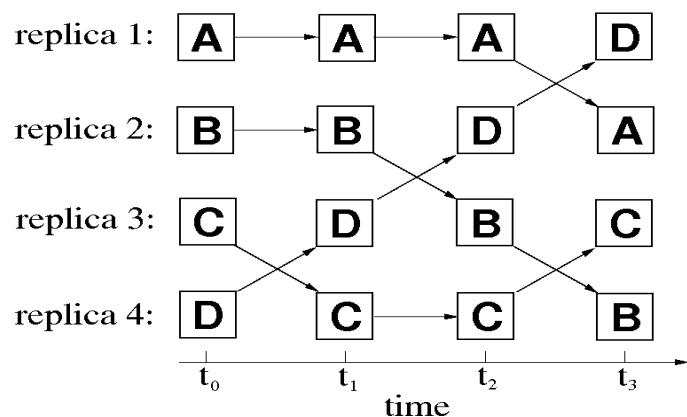
$$\tilde{V}(\mathbf{Q}) = \min\{V(\mathbf{Q})\}$$

Wales, D. J.; Doye, J. P. K., JPCA (1997) 101, 5111-5116

Li, Z.; Scheraga, H. A., PNAS (1987) 84, 6611



Replica exchange molecular dynamics :



Replicas are exchanged according to the canonical **Metropolis criterion** for the exchange probability p :

$$p = \begin{cases} 1 & : \Delta \leq 0 \\ \exp(-\Delta) & : \Delta > 0 \end{cases}$$

$$\Delta = \left(\frac{1}{k_B T_i} - \frac{1}{k_B T_j} \right) (V_i - V_j)$$

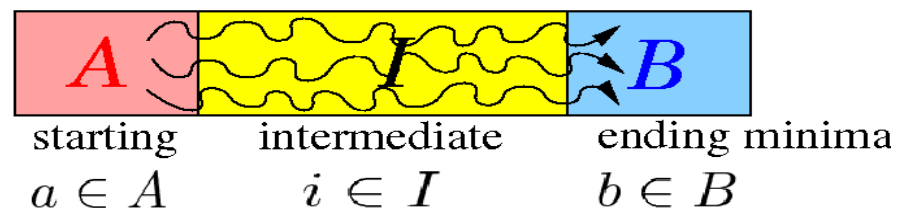
Free energy surfaces (FES) are constructed from the weighted histogram analysis method (**WHAM**).

MMTSB : Brooks, C.L.; Feig, M.; Karanicolas, J., J. Mol. Graph. Model. **22** (2004), 377

WHAM: Kumar et al., J. Comp. Chem. 13 (1992), 1011

Discrete path sampling :

$$k_{BA}^{GT} = \frac{1}{p_A^{eq}} \sum_{a \in A} \frac{p_a^{eq}}{\tau_a} \sum_{b \in B} P_{ba}$$



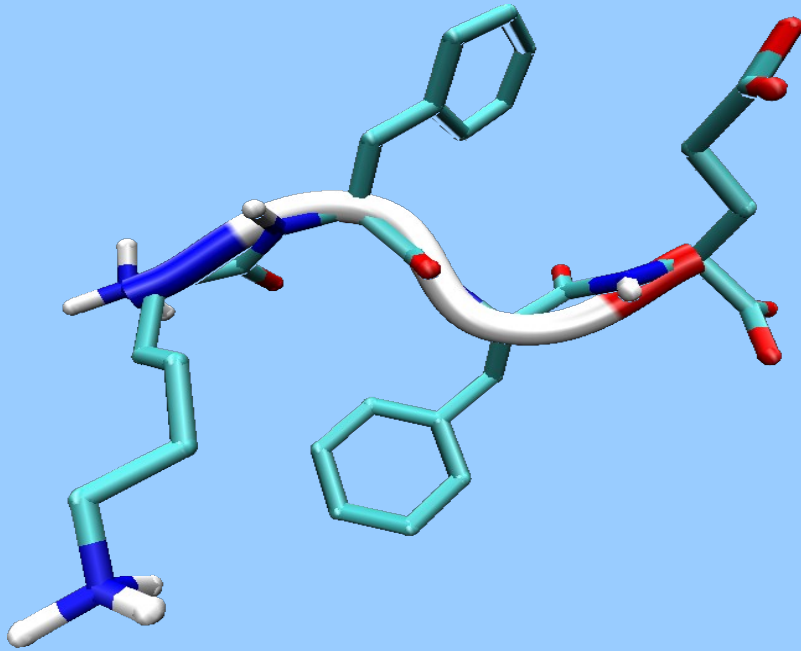
Wales, D. J., Int. Rev. Phys. Chem. (2006), 25 237-282

Example 1 :

KFFE

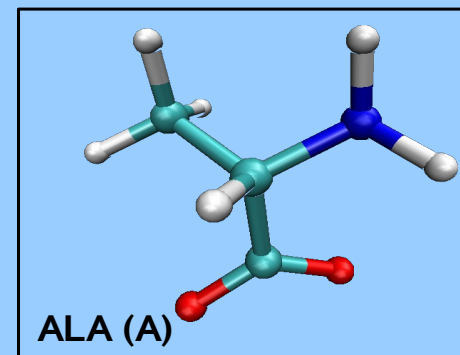
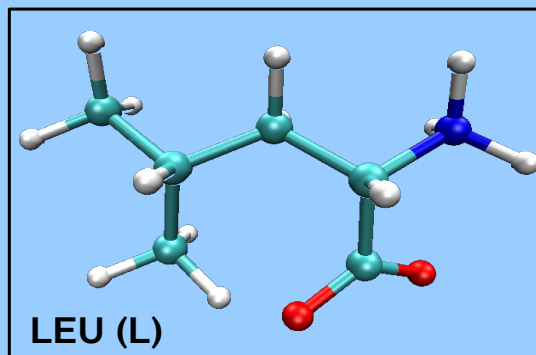
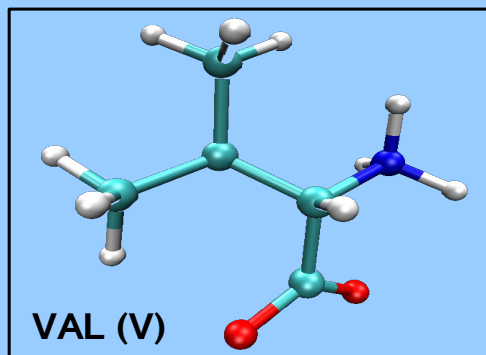
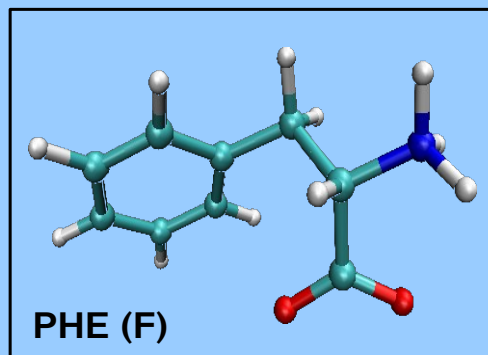
KFFE in experiment

Lys Phe Phe Glu



Experimental study by Tjernberg et al. showed:

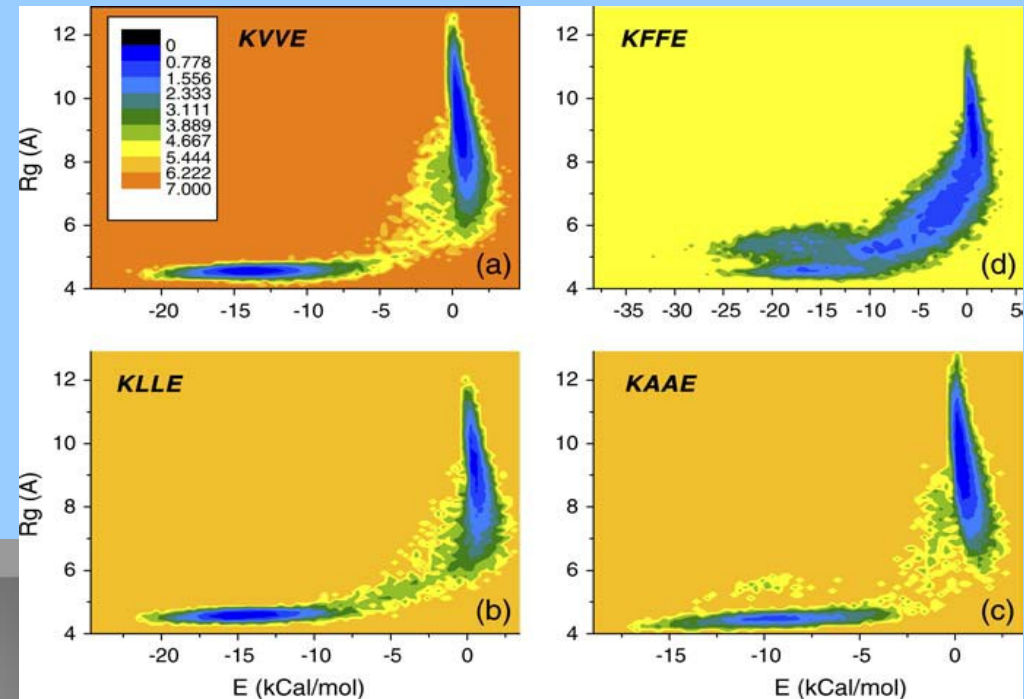
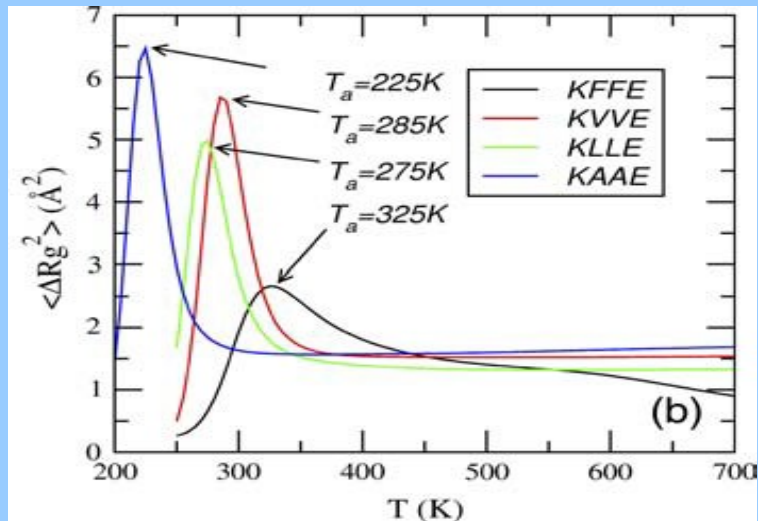
- KFFE and KVVE form amyloid fibrils.
 - KLLLE and KAAE do not form fibrils.
 - KFFK and EFFE do not form fibrils.
 - KFFK + EFFE (1:1) form amyloid fibrils.
 - KFFE and KVVE show partial β -strand conformation in solution.
 - KLLLE and KAAE show random structure only.
- Formation of amyloid fibrils is promoted by complementary interpeptide **electrostatic interactions** and a high **β -propensity** of the monomer.
- No comment on the hydrophobic effect !



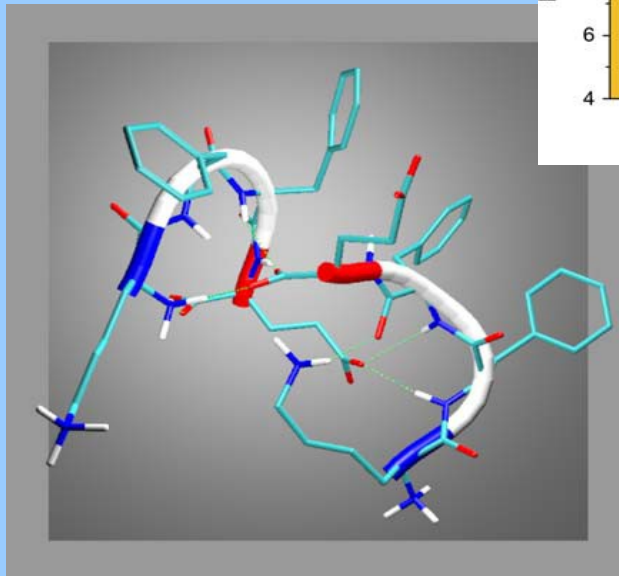
The KFFE dimer

A **theoretical study** by A. Baumketner & J.-E. Shea, in which the **dimerization** of KFFE, KVVE, KLE and KAAE is investigated, mainly supports the experimental results.

The method is **REMD** and as potential was the **CHARMM19** forcefield chosen together with the **Generalized Born** solvation model.



But the most stable KFFE dimer structure is **not sheet-like**:



The KFFE dimer

Our approach : **Global optimization** with different potentials

- 1) CHARMM19 + EEF1
- 2) CHARMM19 + GB
- 3) CHARMM22 + GBSW

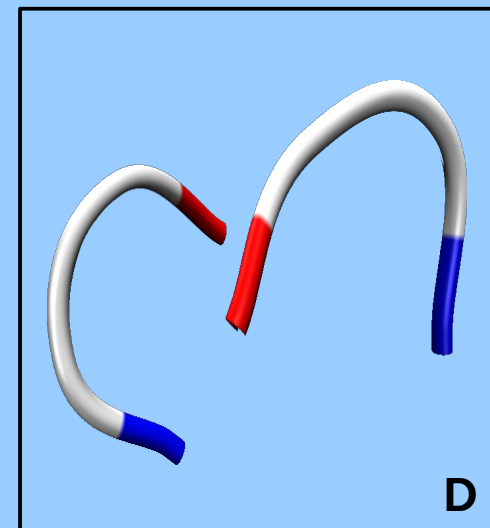
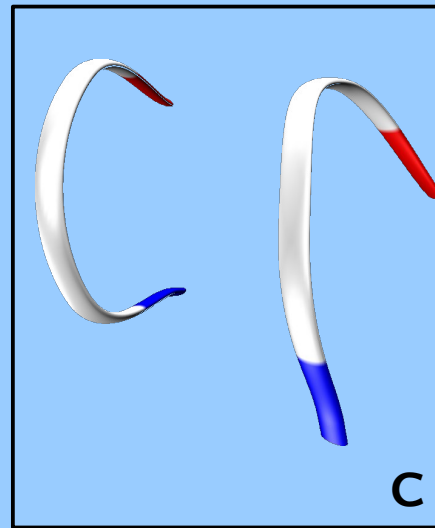
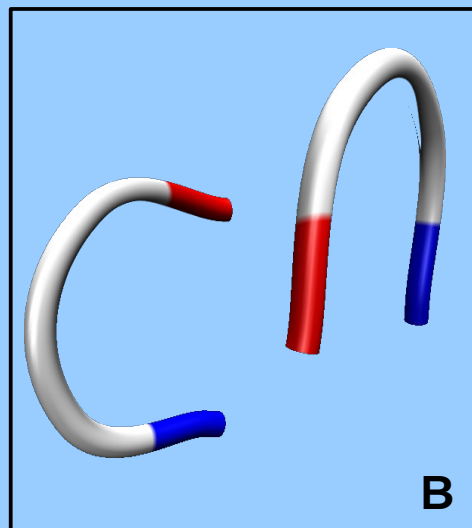
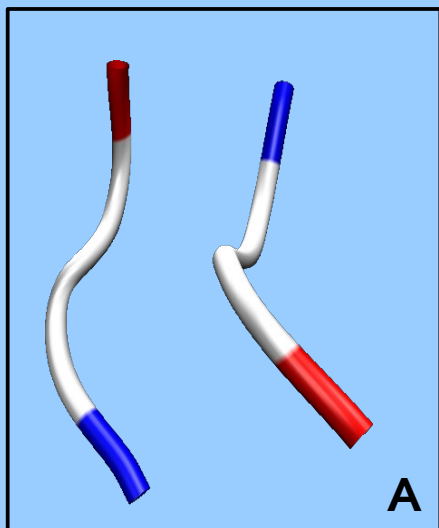
The resulting **lowest-energy structures** from each global optimization run 1) to 3) were then minimized using the other potentials to get an **energy ranking** as a function of the potential.

In addition to the classical force field potentials also **DFT geometry optimizations** were performed for the lowest-energy structures from 1) to 3).

Details of the DFT calculations:

- pbe functional + dnp basis set (= double-zeta basis) as implemented in DMOL3
- COSMO as implicit solvent model

The KFFE dimer



	A	B	C	D
EEF1 energies	0	37.17	14.30	24.12
GB energies	26.36	0	26.25	20.35
GBSW energies	8.18	0.22	0	3.02
DMOL3 energies	1.51	22.34	9.71	0

(all energies in kcal/mol)

The KFFE dimer

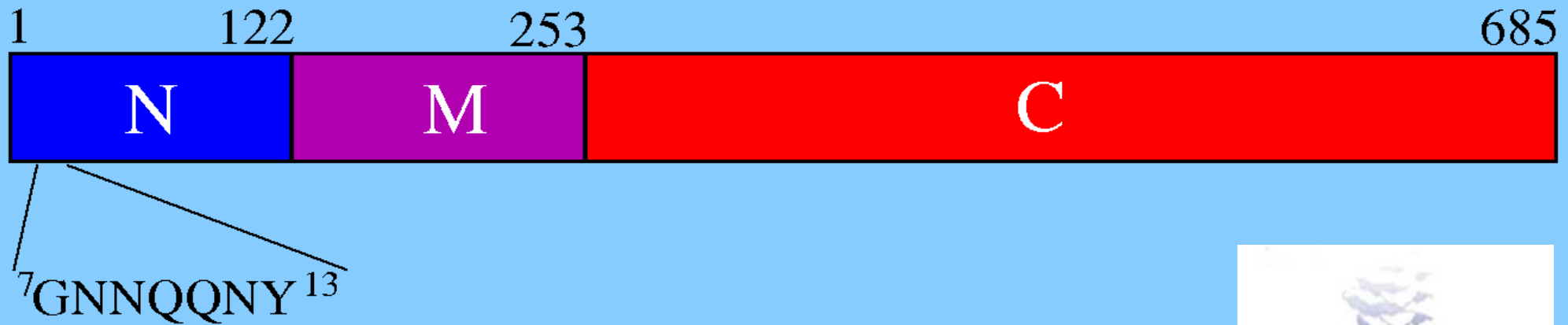
What next ?

- Global minima for **in-vacuo** potentials, i.e. CHARMM19 (with EEF1 parameter file), CHARMM19, CHARMM22 and the DFT energies without COSMO)
- **Free energy surfaces** for different solvent models?
(CHARMM19+EEF1, CHARMM22+GBSW, CHARMM22+TIP3P)
- Origin of different global minima for different potentials / solvent models?
(**Structure analysis**)
- Intermolecular interaction calculated by SAPT/DFT or the distributed-multipole-analysis potential of S. Price & A. Stone
- **Methodological developments** for the MC step taking scheme to improve the sampling of peptide oligomers.

Example II :

GNNQQNY

GNNQQNY – a 7-residue peptide from Sup35



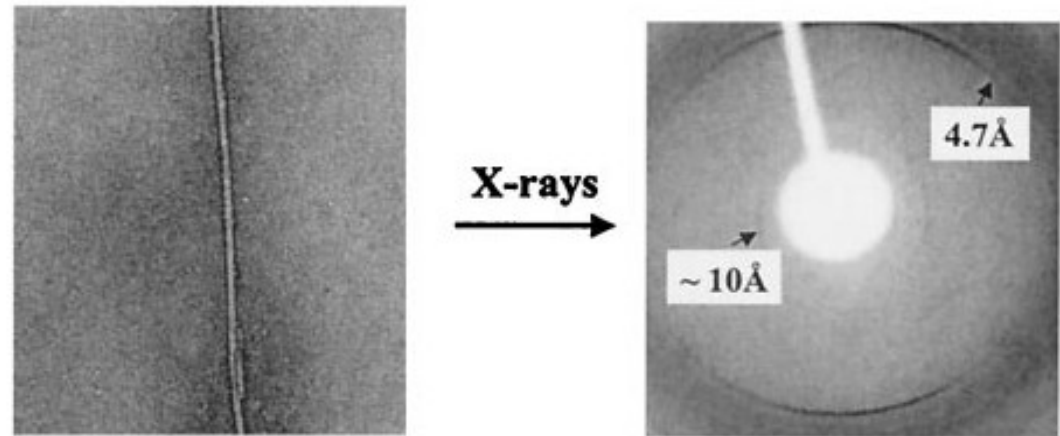
- **Sup35** is a 685-residue **prion-like** protein in yeast
- Residues **1-122** are the **prion-determining** domain (**N region**), which contains a series of 9-residue repeats with sequence PGGGYQQYN.
- Residues 123-253 are the highly charged M region, and residues 254-685 function in **translation termination** (Sup35's **normal** cellular role).
- **GNNQQNY** is a 7-residue polar peptide **from the N region** that exhibits the **amyloid** properties of full-length Sup35:
 - cooperative kinetics of aggregation with a concentration-dependent lag time
 - binding of the dye Congo red
 - the characteristic cross- β - x-ray diffraction pattern



Amyloid fibrils from the NM region of Sup35.
[Nature 435 \(2005\), 765](#)

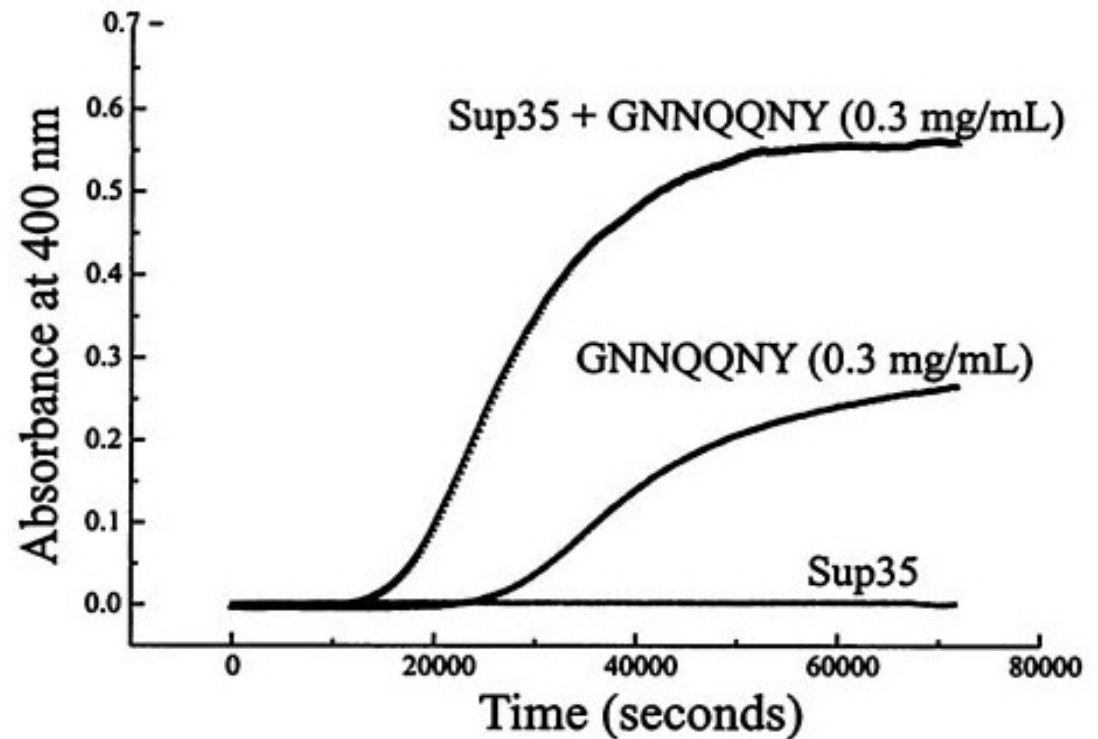
Amyloid fibrils of GNNQQNY

An electron micrograph of the GNNQQNY amyloid fibrils and their x-ray diffraction pattern.



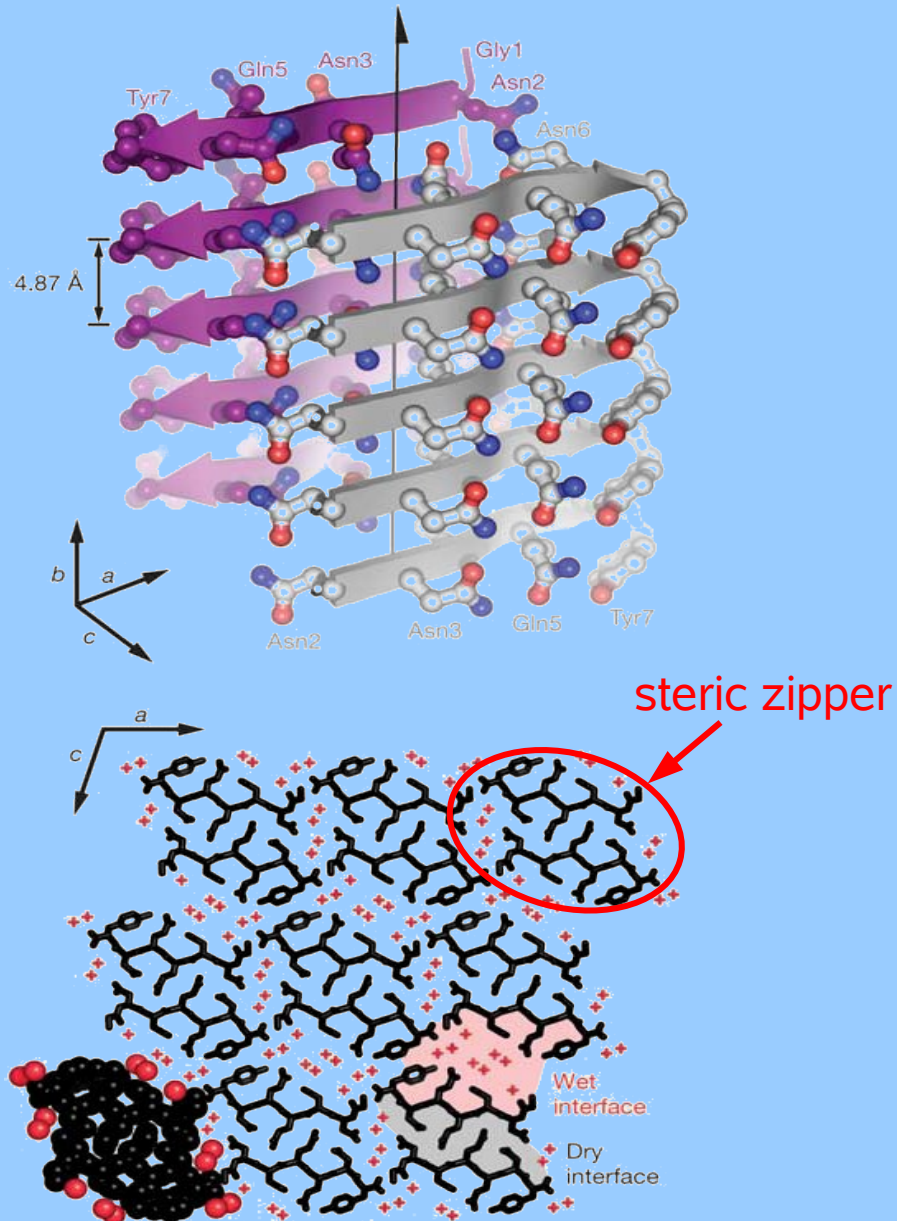
Fibril diameter $\sim 75\text{\AA}$

Kinetics of amyloid formation for GNNQQNY, Sup35 and a mixture of both.

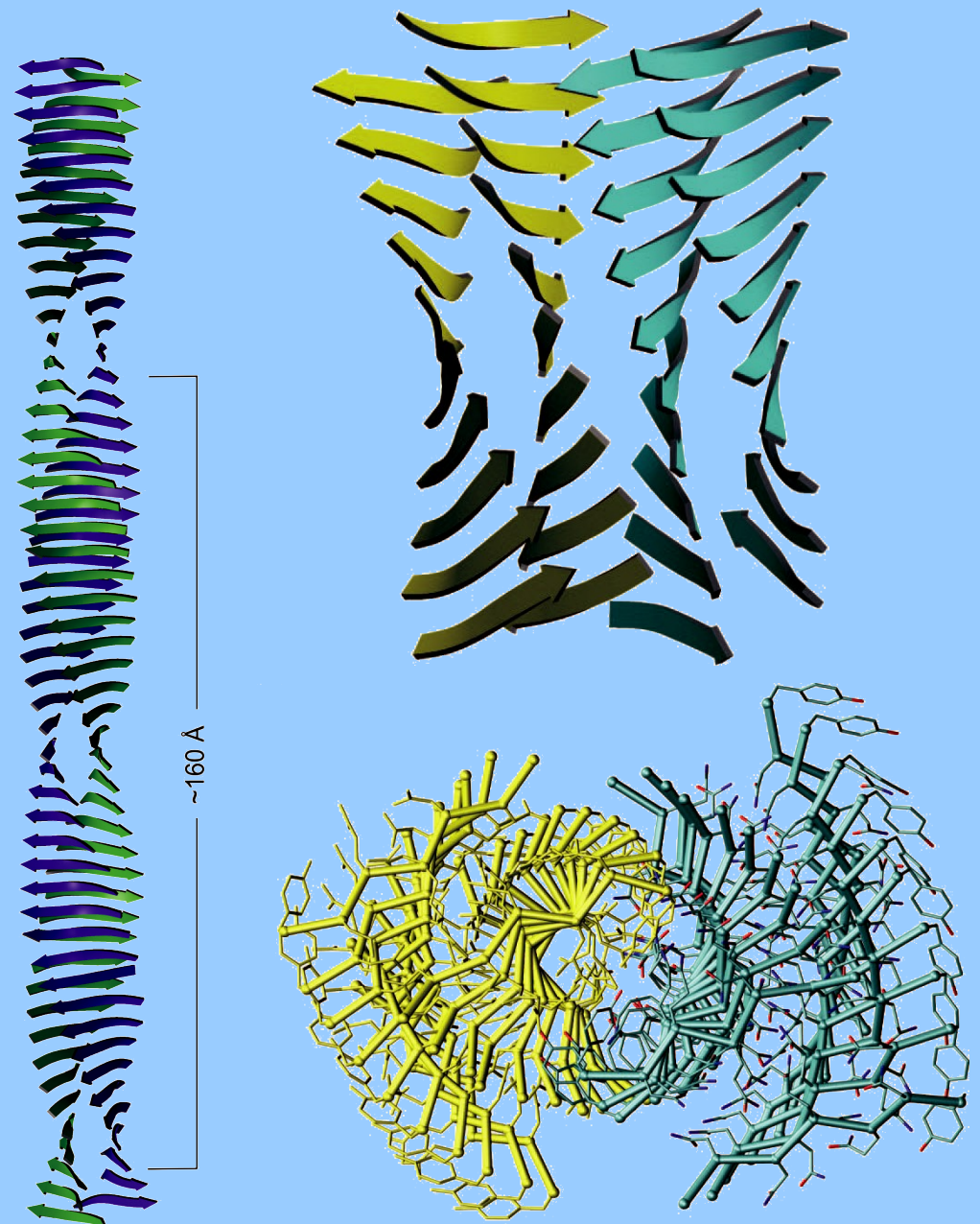


Amyloid fibrils of GNNQQNY

Experiment : (PDB 1YJP)



Theoretical study :

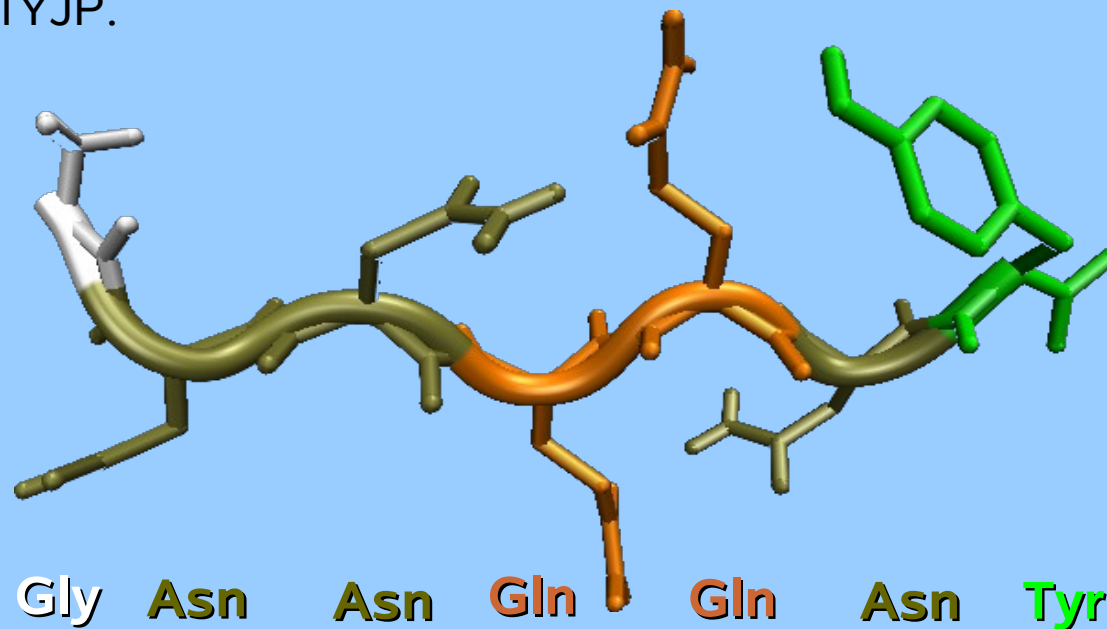


The GNNQQNY monomer

Motivation :

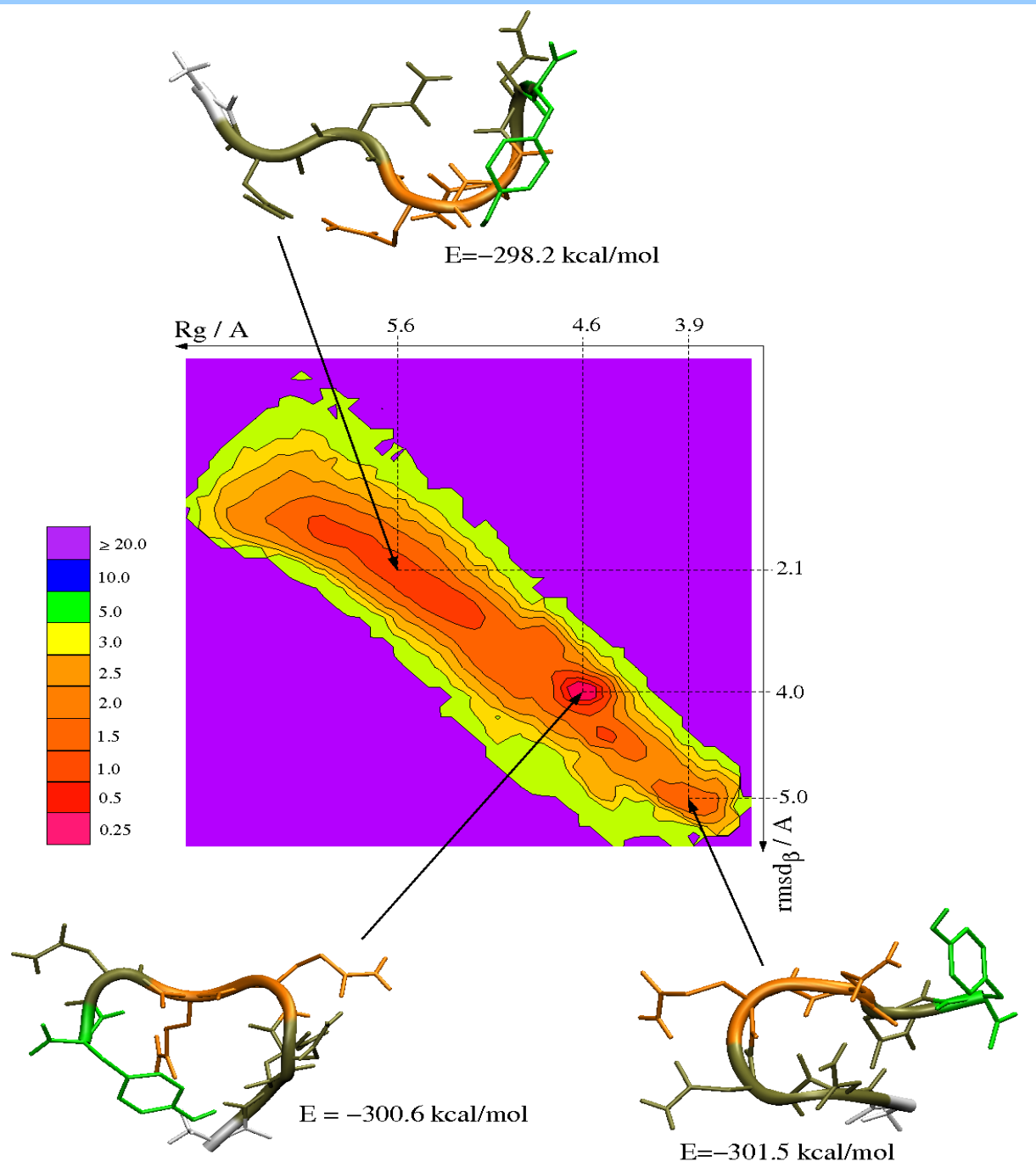
- To study the monomer was motivated by a simulation done by R. Pellarin & A. Caflisch in which they had used a coarse-grained model of an amphipathic polypeptide to investigate **kinetics of aggregation and the pathways of fibril formation**.
- They found that with **increasing** relative **stability of the β -prone state** of the polypeptide, **disordered aggregation** changes into **fibrillogenesis** with oligomeric **on-pathway** intermediates, and finally **without intermediates** for very stable β -prone peptides.
- R. Pellarin & A. Caflisch suspect **GNNQQNY** belonging to the class of very stable **β -prone** peptides and thus should exhibit very **fast fibrillogenesis**.

Starting structure : A β -strand which is the building block of the amyloid structure, taken from PDB 1YJP.

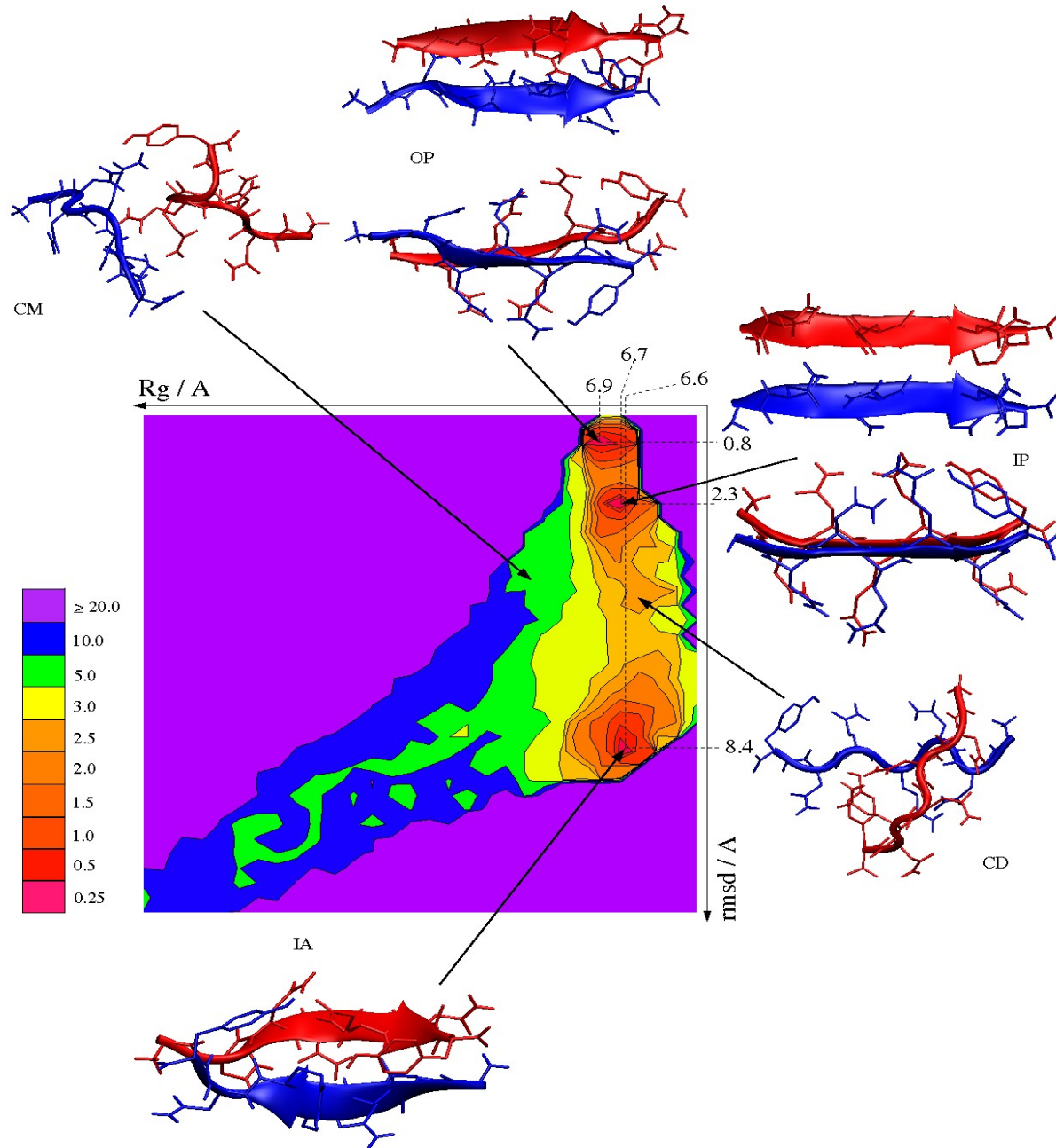


The GNNQQNY monomer

- CHARMM19 + EEF1
- 100-ns REMD with 8 replicas between 250 and 400 K
- FES for T=298 K, order parameters:
 - i) radius of gyration
 - ii) C_{α} -RMSD from the β -strand

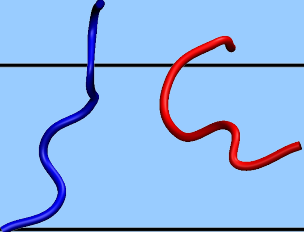
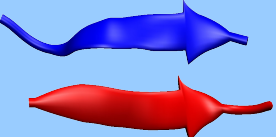
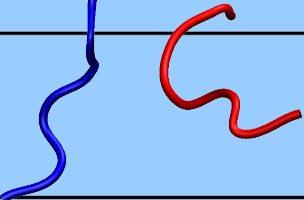
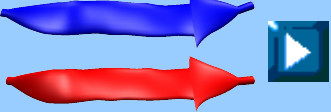

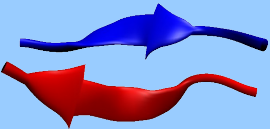
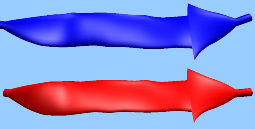
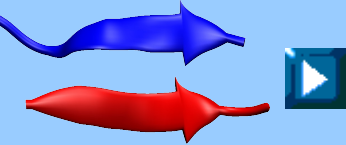
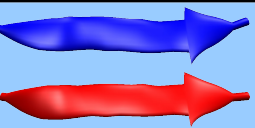
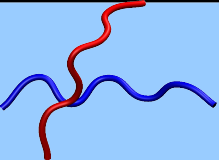
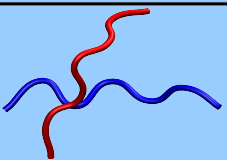
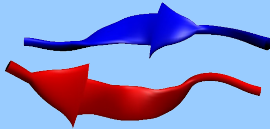


The FES of the GNNQQNY dimer

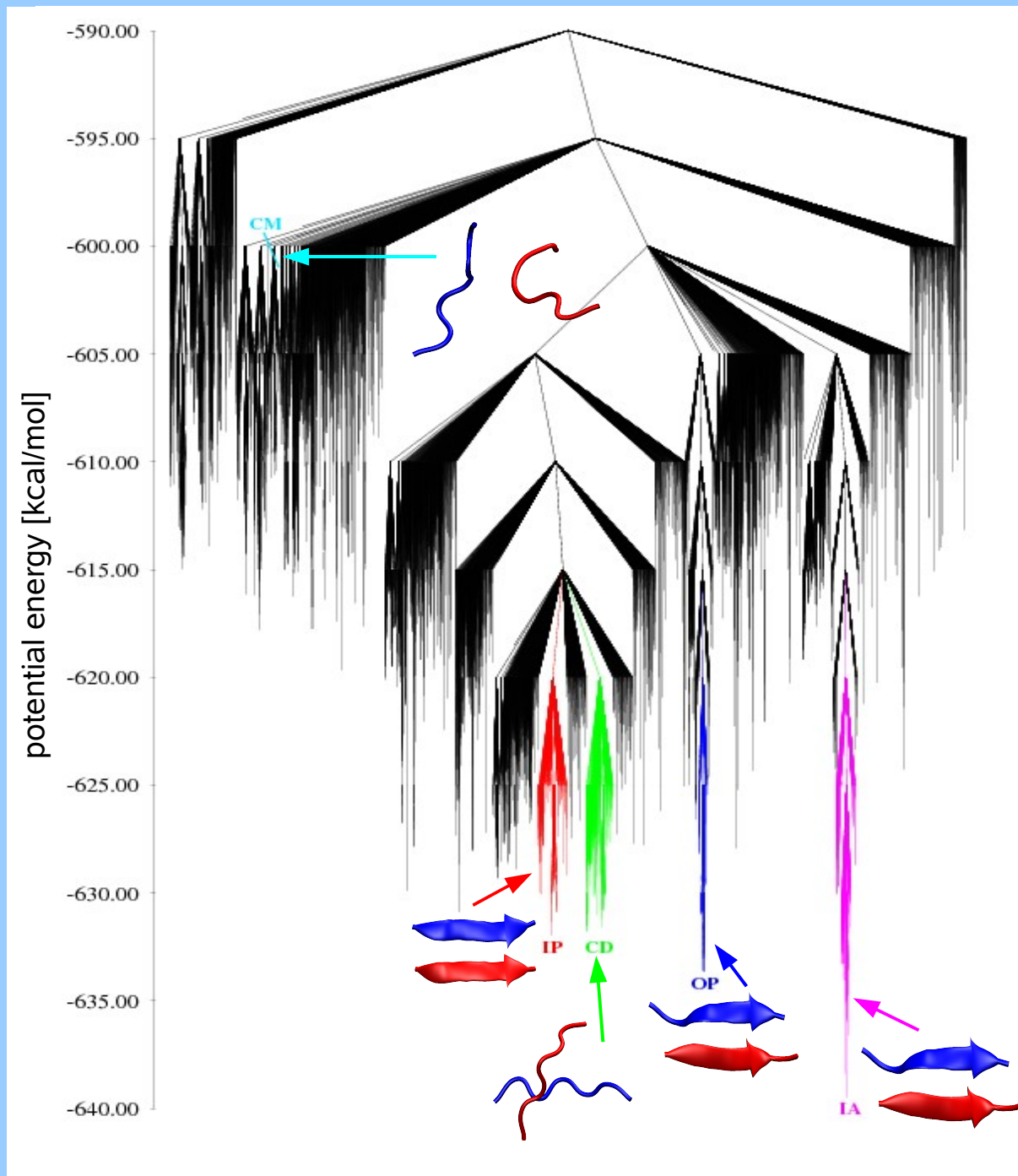


- CHARMM19 + EEF1
- 100-ns REMD with 16 replicas between 220 and 600 K
- concentration of 10 mM
- FES for T=298 K, order parameters:
 - i) radius of gyration
 - ii) C_α -RMSD from the off-register, parallel dimer (OP) (found in a global optimization run)

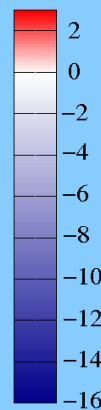
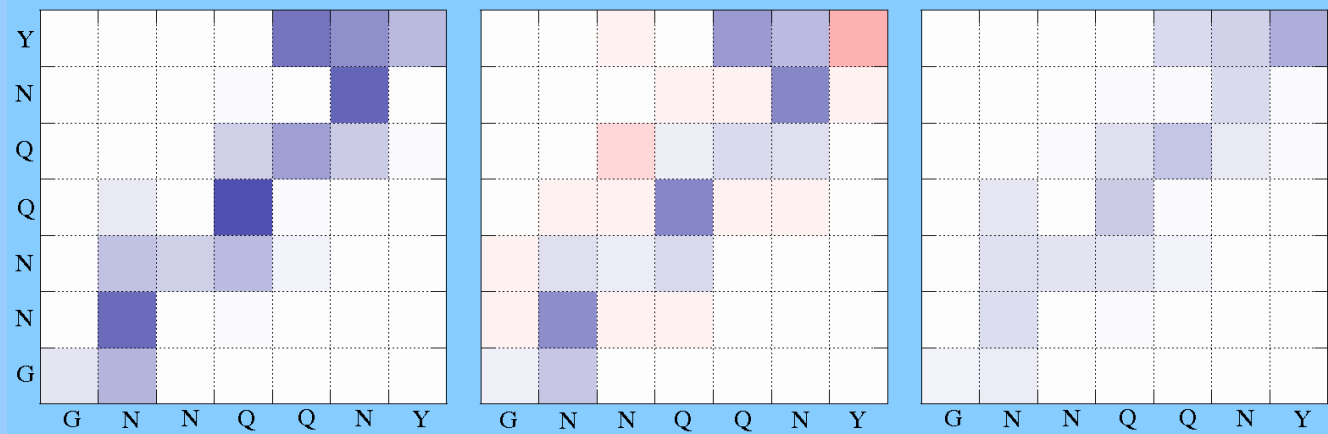
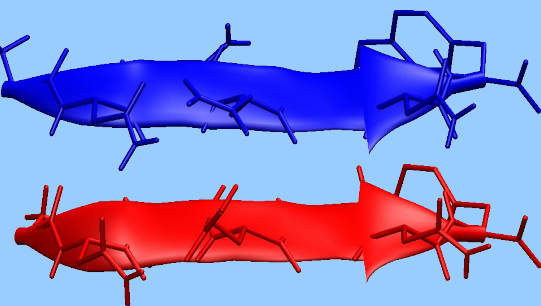
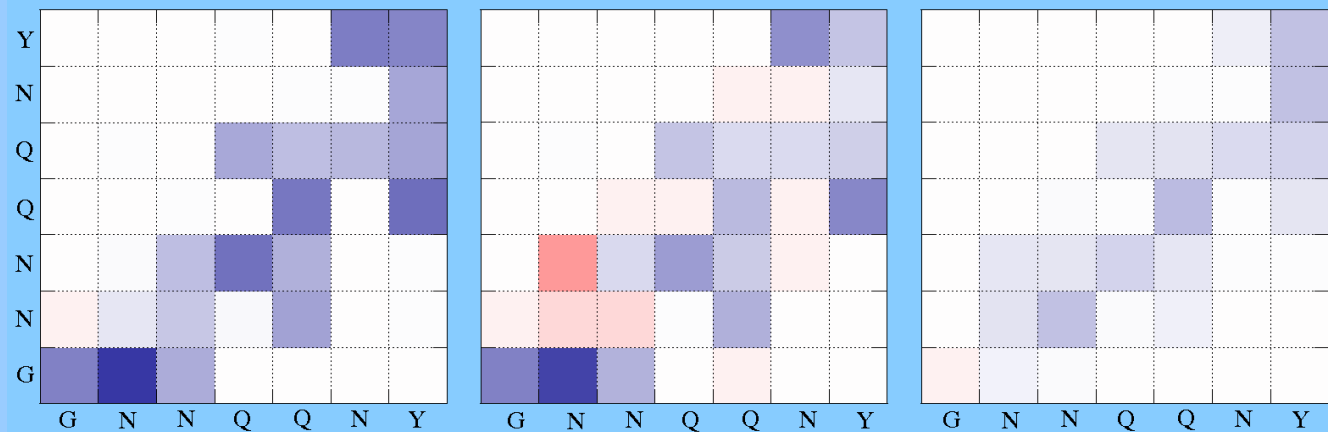
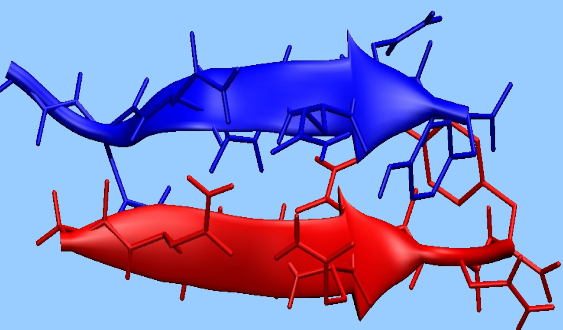
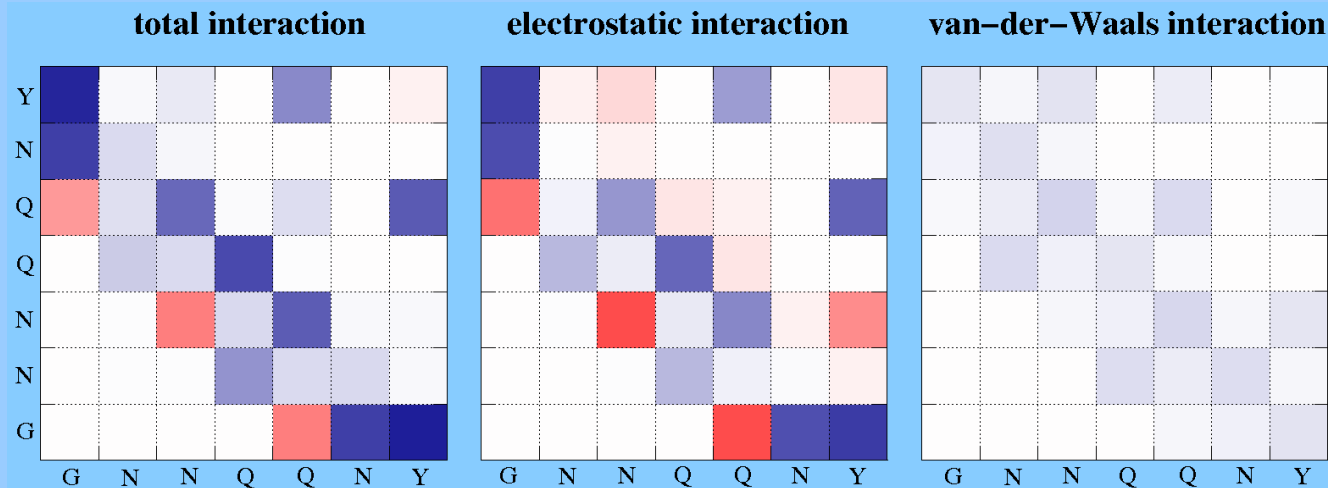
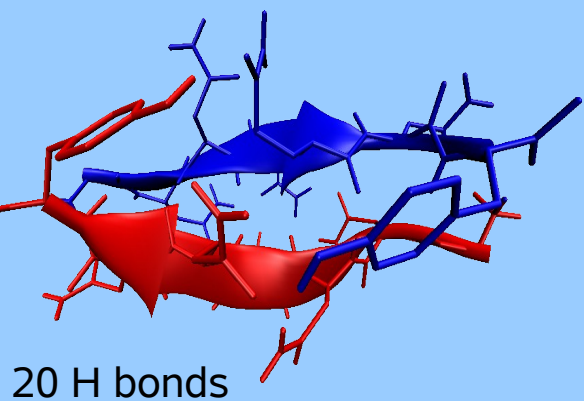
DPS for the GNNQQNY dimer

<i>A</i>	<i>B</i>	$k_{B \leftarrow A}^{\text{GT}} / \text{s}^{-1}$	$k_{A \leftarrow B}^{\text{GT}} / \text{s}^{-1}$
		10^{+4}	10^{-8}
		10^{-1}	10^{-11}
		10^{-2}	10^{-11}
		10^{-7}	10^{-6}
		10^{-2}	10^{+4}
		10^{-4}	10^{-6}

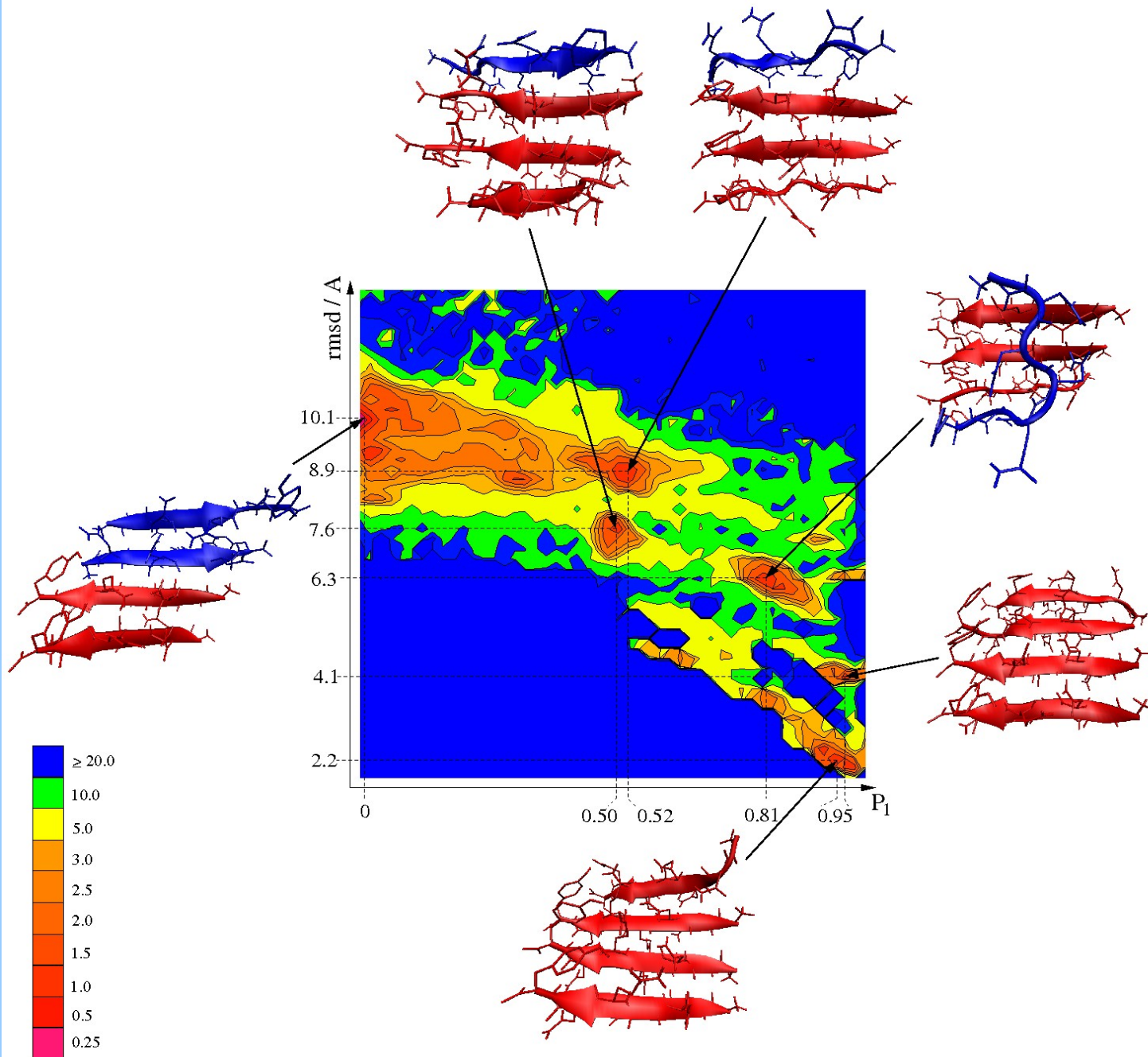
Disconnectivity graph for the GNNQQNY dimer



Interaction energy for the GNNQQNY dimer



The GNNQQNY tetramer



- CHARMM19 + EEF1
- 100-ns REMD with 16 replicas from 220 to 600 K
- concentration of 10 mM
- FES for T=298 K, order parameters:

i) C_α -RMSD from the β -sheet tetramer (PDB structure)

ii) polar order parameter

$$\langle P_1 \rangle = \frac{1}{N} \sum_{i=1}^N \mathbf{z}_i \cdot \mathbf{d}$$

\mathbf{d} director

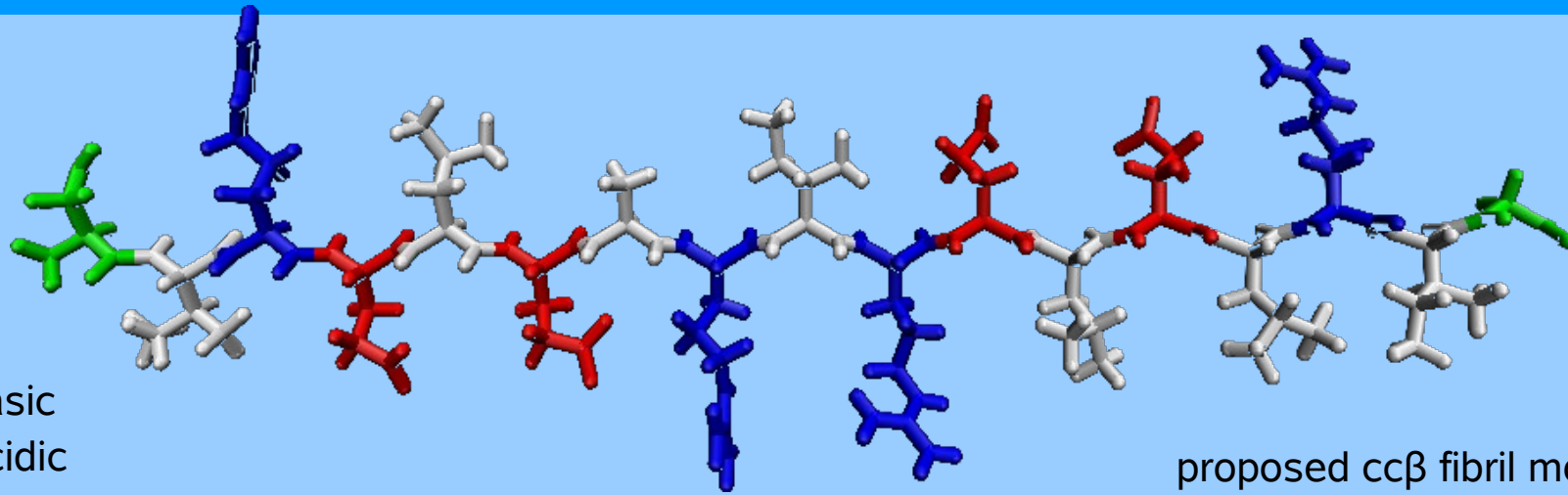
\mathbf{z}_i end-to-end vector of peptide i

Example III :

ccβ

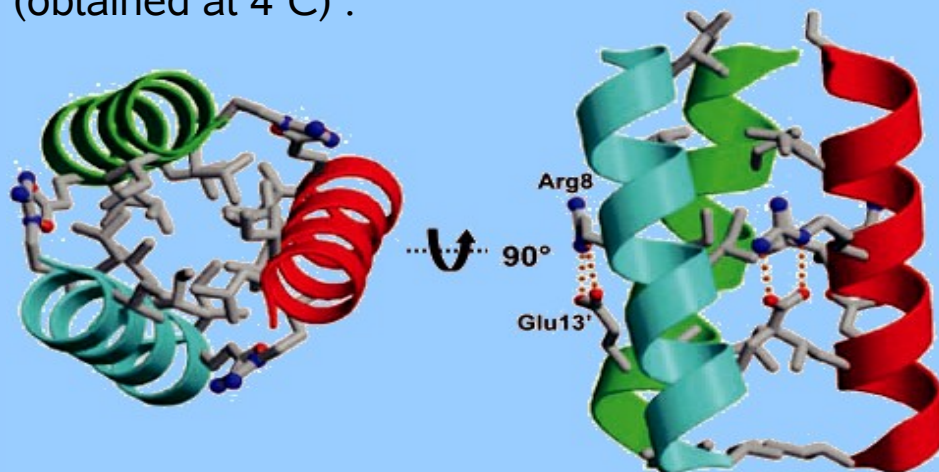
Amyloid formation by cc β

SER-ILE-ARG-GLU-LEU-GLU-ALA-ARG-ILE-ARG-GLU-LEU-GLU-LEU-ARG-ILE-GLY

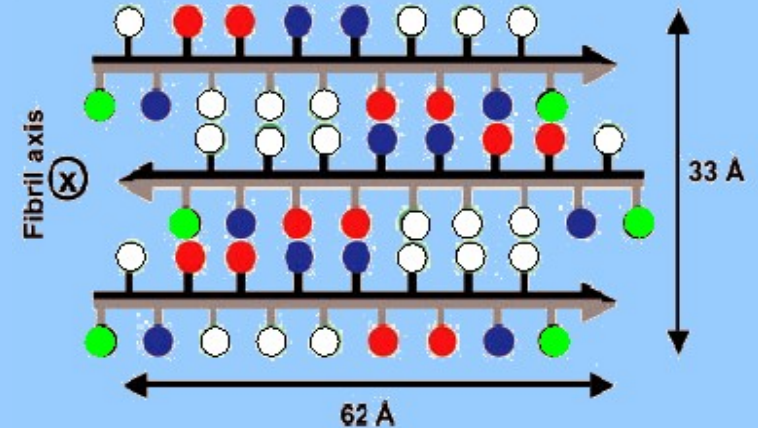
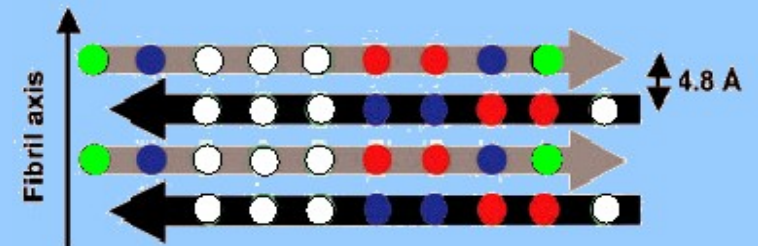


- basic
- acidic
- hydrophobic
- polar

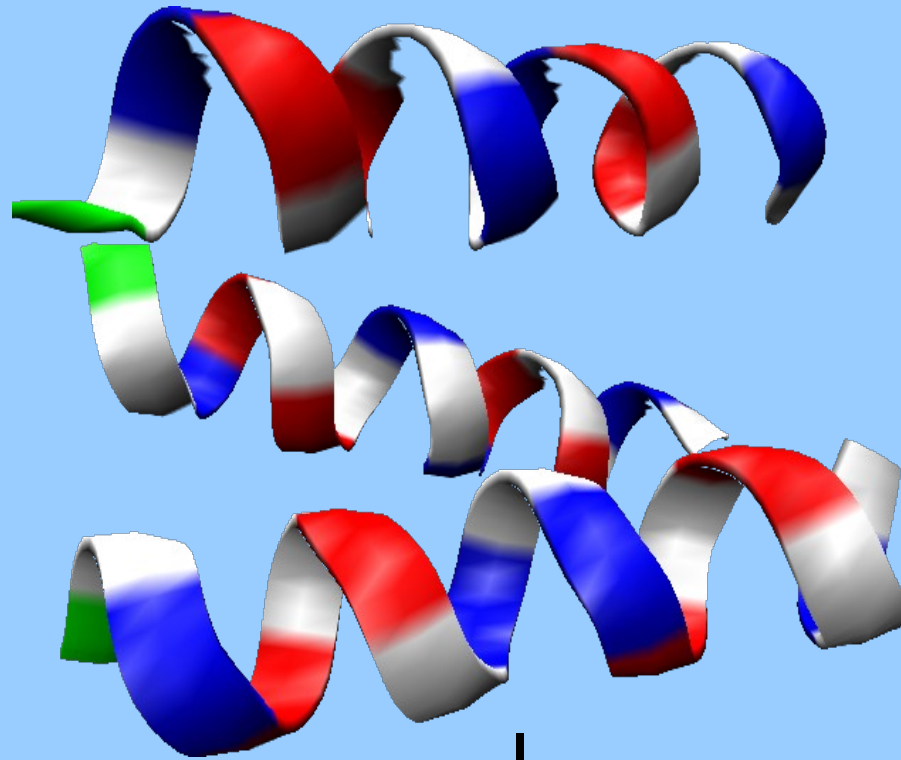
crystal structure of cc β
(obtained at 4°C) :



proposed cc β fibril model
(obtained at 37°C) :

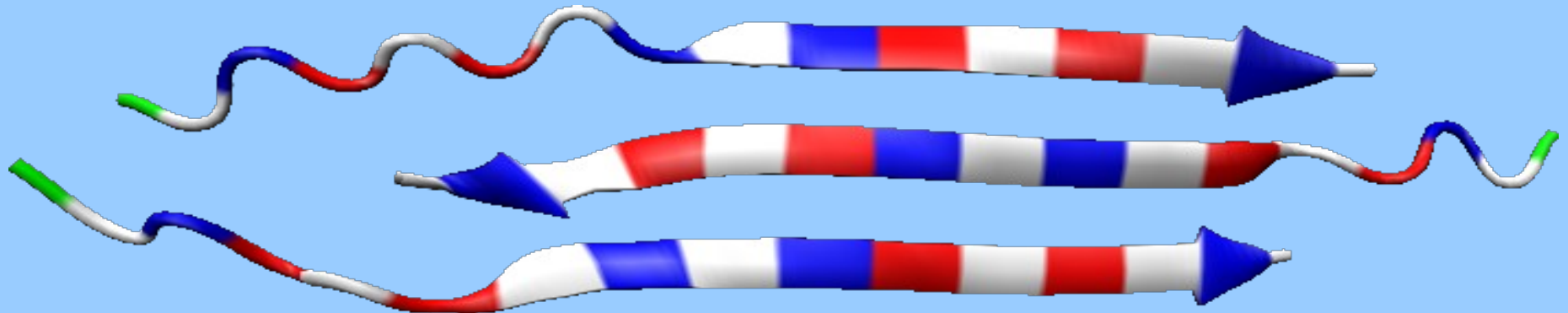


Amyloid formation by cc β



pathway ?

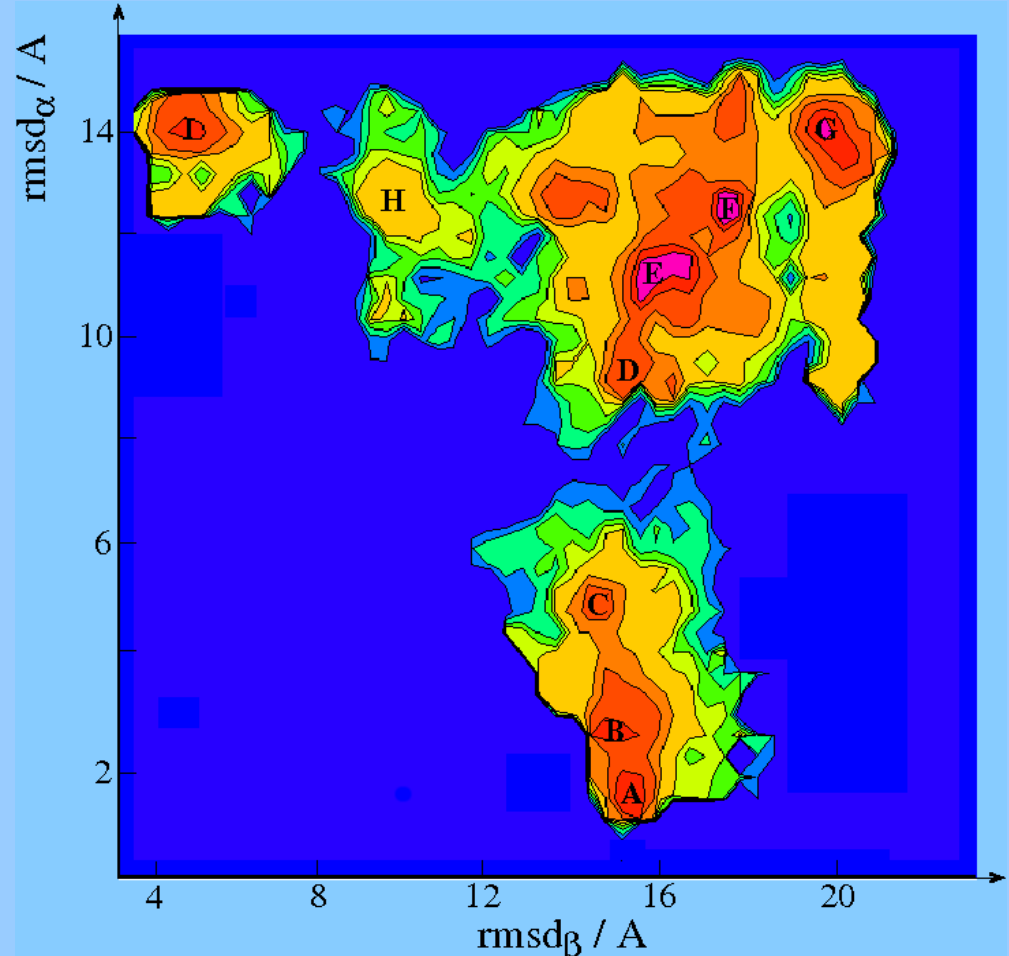
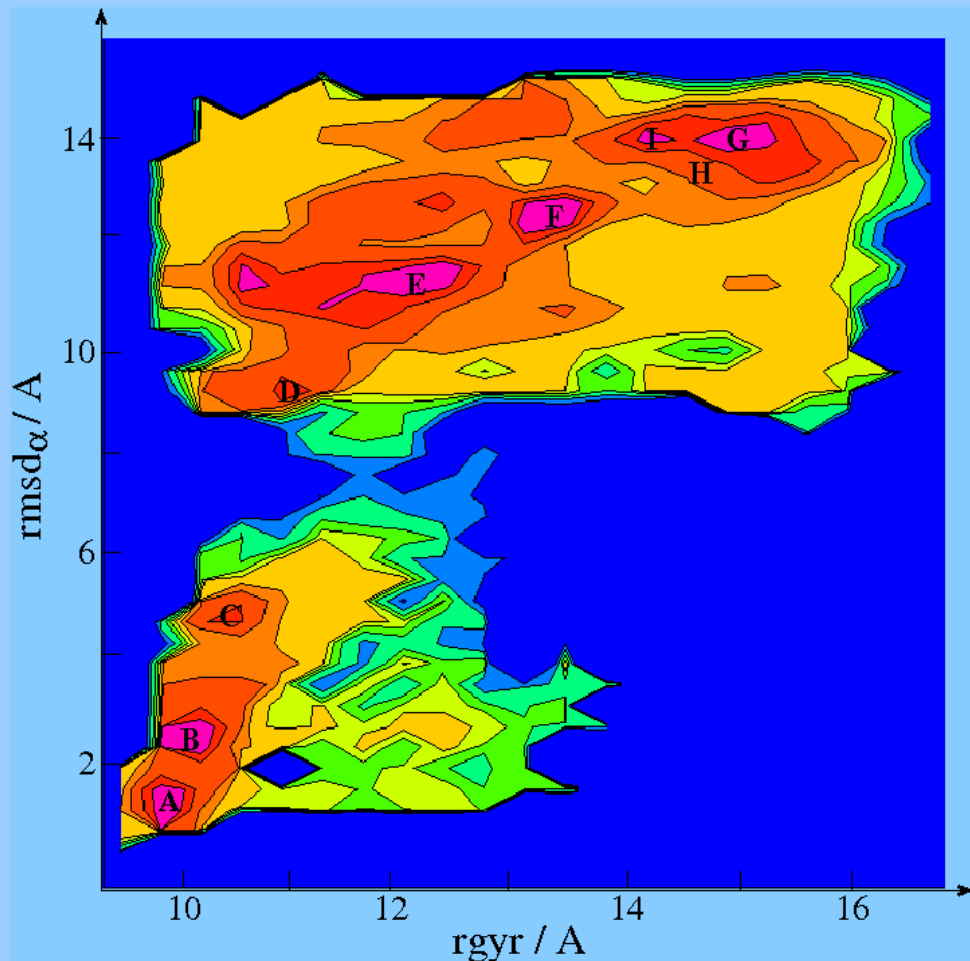
β -sheet constructed with CNSsolve,
fulfills NMR data from Kammerer *et al.*:



REMD for the cc β trimer

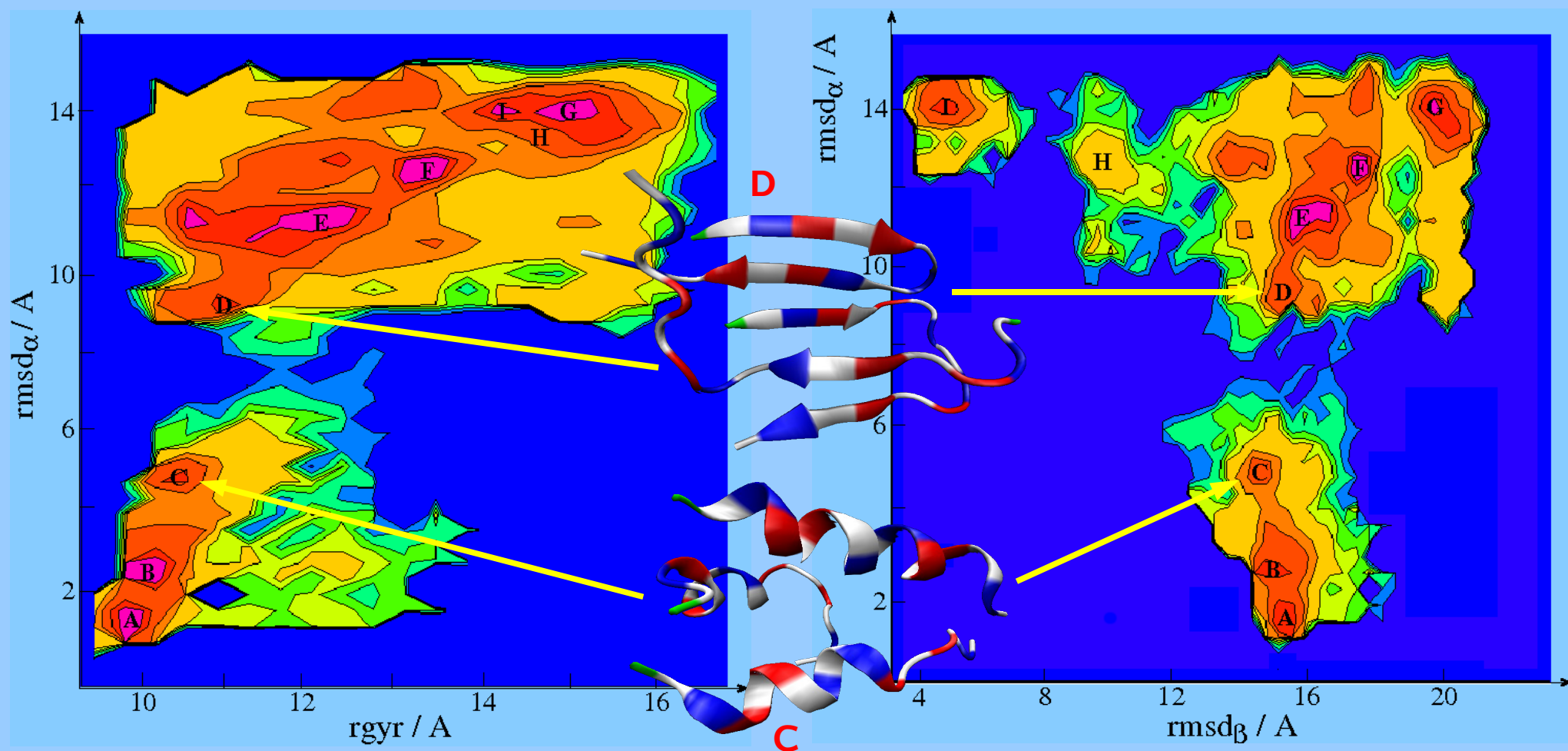
WHAM free energy surfaces at 310 K :

- CHARMM19 + EEF1
- 100 ns REMD with 16 replicas between 220 and 600 K
- concentration of 10 mM
- order parameters: RMSD from α -helix trimer, RMSD from β -sheet and radius of gyration (rgyr)

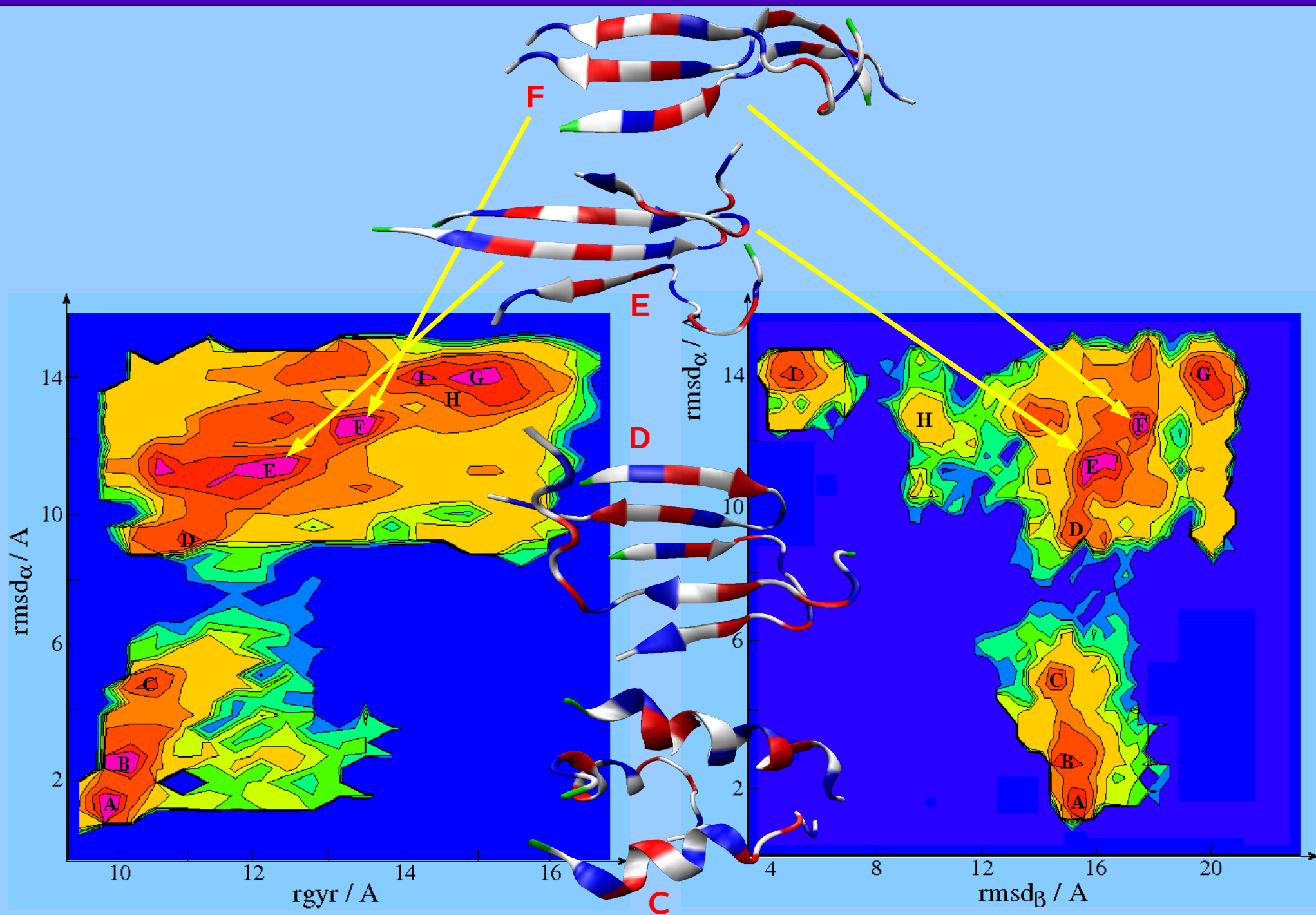


What structures dominate the free energy surface ?

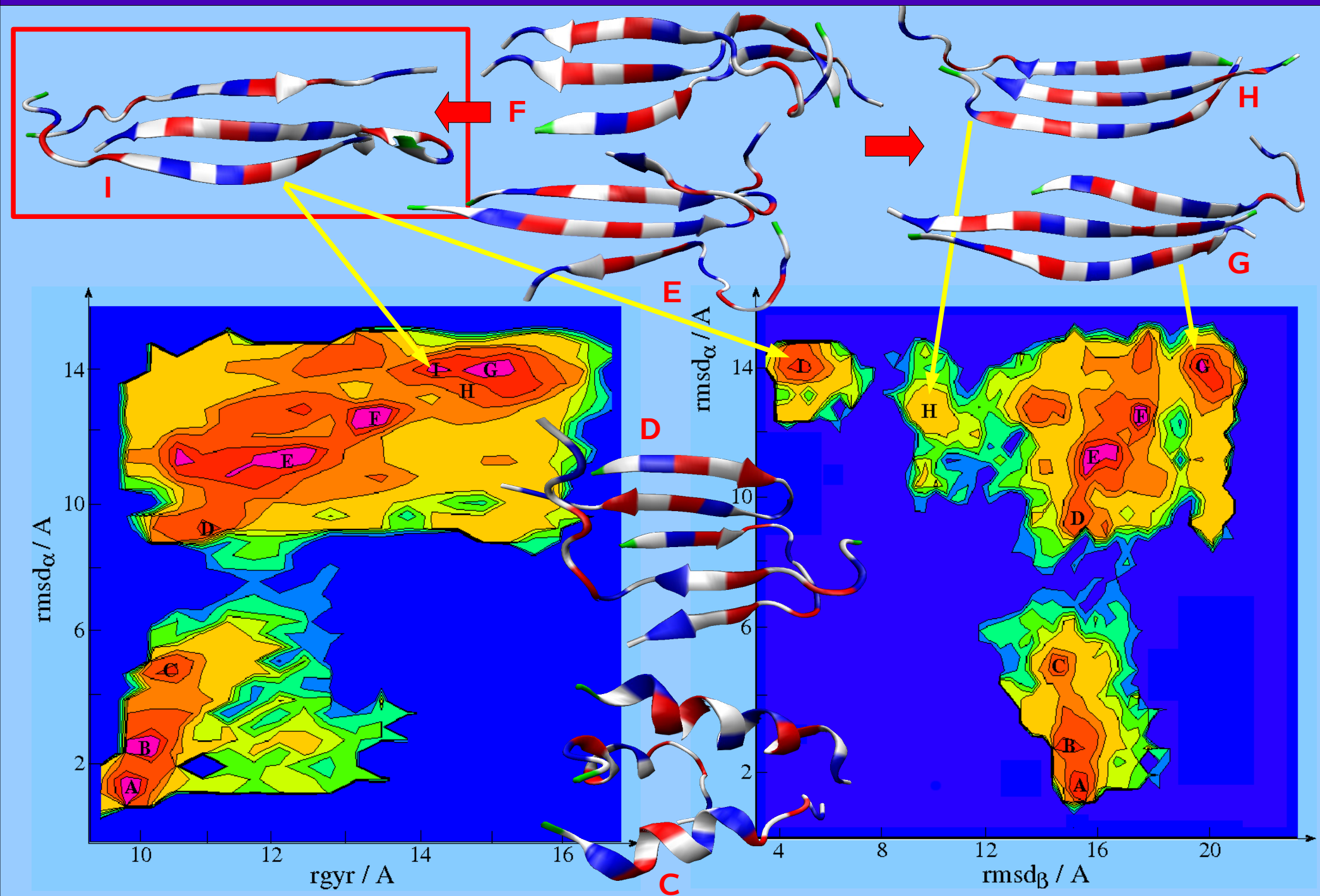
FES for the cc β trimer



FES for the cc β trimer



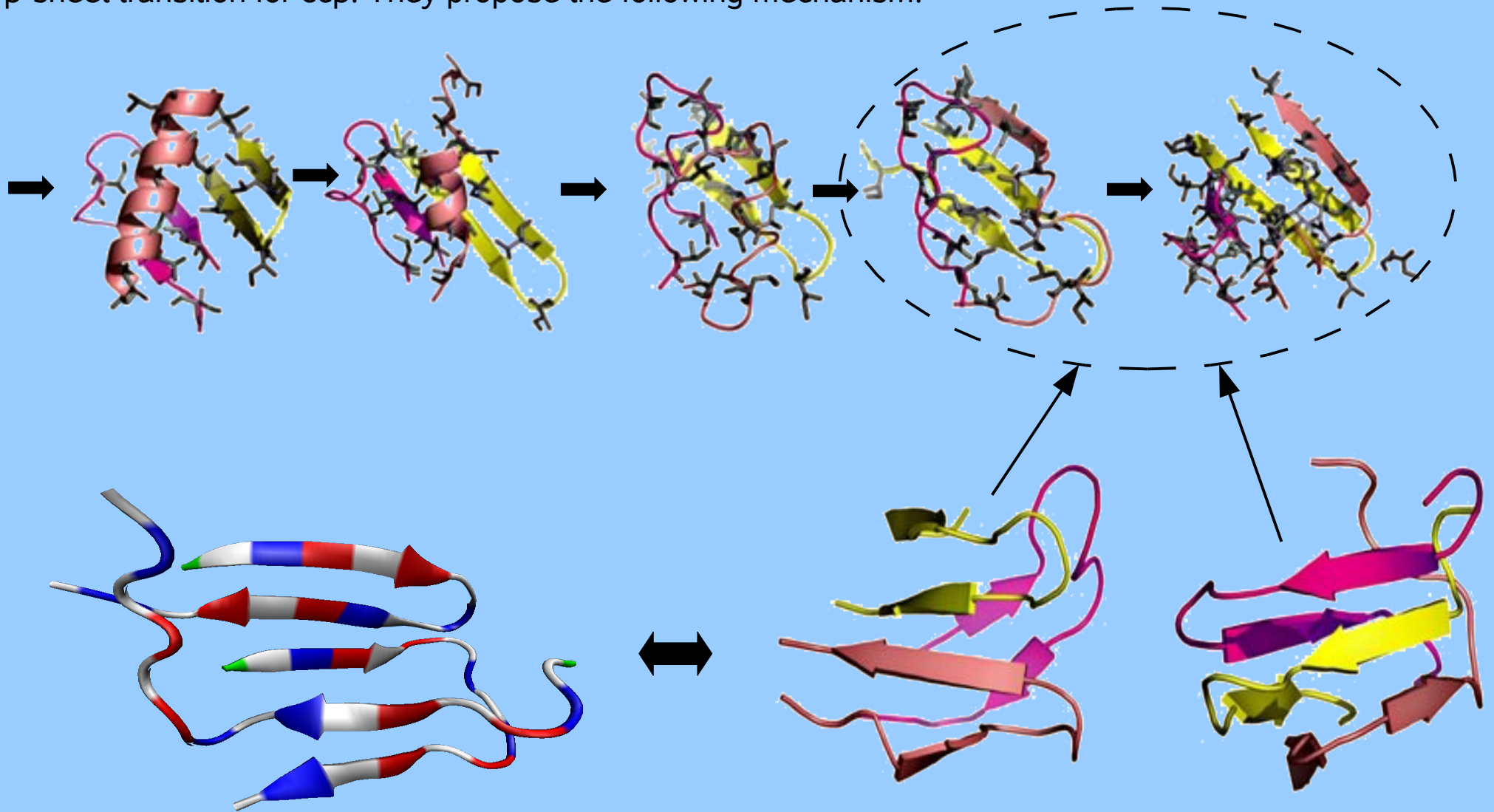
FES for the cc β trimer



Amyloid formation by cc β

β -hairpin aggregate as intermediate ?

N. V. Dokholyan and co-workers did an MD study with a coarse-grained potential to study the α -helix to β -sheet transition for cc β . They propose the following mechanism:



Future projects

Future Projects

KFFE : Free energy surfaces for the KFFE dimer using different potentials and solvent models.

Origin of the structural differences.

GNNQQNY : Finishing the tetramer study.

Studying the octamer.

cc β : Finding a pathway with $k \geq 10^{-8}$ 1/s.

Comparison of self-assembly pathways for amyloidogenic hepta- and octapeptides with different hydrophobicity.

Methodological developments to improve Basin Hopping and Discrete Path Sampling for the exploration of amyloid formation.

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